

College of Engineering
Department of Electrical and Computer Engineering

332:322

Principles of Communications Systems

Spring 2006

Quizlette I

FOR FUN, NOT FOR CREDIT**BUT:** if you don't get a high score on this, you should worry1. (30 points) **Linear Systems:**

- (a) (10 points) Once again write down the forward and reverse Fourier Transform which relates $x(t)$ and its Fourier Transform $X(f)$.
- (b) (20 points) Show that if $x(t)$ has Fourier Transform $X(f)$, then the Fourier Transform of $x(t - t_0)$ is $e^{-j2\pi f t_0} X(f)$.

2. (30 points) **Amplitude Modulation:**

- (a) (10 points) What is the Fourier Transform of $m(t) \cos 2\pi f_c t$ given the Fourier Transform of $m(t)$ is $M(f)$?
- (b) (10 points) What is the Fourier Transform of $m(t) \cos 2\pi f_c t + jm(t) \sin 2\pi f_c t$ given the Fourier Transform of $m(t)$ is $M(f)$?
- (c) (10 points) The previous part is an (unrealizable) form of what sort of modulation?

3. (30 points) **Quantization:**

- (a) (10 points) What is the purpose of a quantizer? State your answer in words (no more than a short paragraph). NOTE: this is not an *optimality* question, just a simple question about what a quantizer is used for.
- (b) (10 points) The Lloyd-Max conditions for optimal quantization are $q_k = E[X|X \in A_k]$ where A_k is the event that random variable $X \in (x_{k-1}, x_k)$ and $x_k = \frac{1}{2}(q_k + q_{k+1})$. Suppose $f_X(x) = [u(x+1) - u(x-1)]/2$. Is a 1 bit quantizer with $q_0 = -0.5$, $q_1 = 0.5$ and $x_0 = 0$ optimal? Why/Why not?
- (c) (10 points) Sketch the output to this quantizer on the interval $t \in (0, 6)$ when the input is the sawtooth waveform

$$m(t) = u_{-2}(t) + 2 \sum_{k=0}^{\infty} (-1)^k u_{-2}(t - 2k + 1)$$

where $u_{-2}(t)$ is the unit ramp (the integral of the unit step). Then provide an analytic expression for $Q(m(t))$ in terms of the unit step function $u(t)$ (also known as $u_{-1}(t)$ in some circles).