

## School of Engineering Department of Electrical and Computer Engineering

## **332:221** Principles of Electrical Engineering I Ouizlette 11

Fall 2012

USING A CALCULATOR WILL SLOW YOU DOWN! Final answers must appear in the appropriate box. Show your work outside the box.

1. Basic Then ... Not Basic:



Assume sinusoidal steady state operation at some frequency  $\omega$ .

(a) (2pts) What value of Z maximizes the average power transferred to Z?

$$Z = Z_{th}^* = R - Lj\omega - \frac{1}{Cj\omega}$$

(b) (3 pts) Suppose we require  $Z = R_L$  to be real (i.e., just a regular old resistor). What value of  $R_L$  maximizes power transfer into Z?

Let 
$$Z = R_L$$
 and  $Z_{th} = R + jX$ 

$$\overline{P} = \frac{1}{2} |V|^2 \frac{R_L}{(R_L + R)^2 + X^2}$$

Differentiating and setting equal to zero gives

$$R_L = |Z_{th}|$$

- 2. Your Cute Future: Consider the circuit shown in the figure.
  - (a) (1 pt) Assume the input voltage source amplitude is  $V_1 = V_1$  where  $V_1 \in \Re$  and that the frequency of operation is  $\omega$ . Please provide a labeled sketch of  $V_2(t)$ .



$$V_2(t) = V_1 \frac{\mathbf{sgn}(\cos\omega t) + 1}{2} \cos\omega t$$

(b) (1 pts) Can you provide a transfer function from  $V_1$  to  $V_3$ ? Why?/Why not?

Nope. The circuit is nonlinear.

(c) (1 pts) If  $\omega = 2\pi \cdot 60$  and  $R = 10k\Omega$ , provide (and argue for) a value of C that makes  $V_3(t) \approx V_1$ ? **HINT:** Remember that RC is called the "time constant" and is a measure of how quickly charge bleeds from a capacitor C through a resistor R.

We need  $RC \gg 1/60$  so say RC = 1/6 or C = 1/60000whatever that is.

(d) (2 pts) You are told that

$$V_2(t) = V_1 \sum_{k=-\infty}^{\infty} \frac{\cos \frac{k\pi}{2}}{\pi (1-k^2)} e^{jk\omega t}$$

is the analytic form of what you SHOULD have sketched in the previous part :) :) . What is the output  $V_3(t)$ .

Superposition holds to the right of 
$$V_2(t)$$
 so  

$$V_3(t) = V_1 \sum_{k=-\infty}^{\infty} |H(jk\omega)| \frac{\cos \frac{k\pi}{2}}{\pi(1-k^2)} e^{jk\omega t + j \angle H(jk\omega)}$$
where  $H(j\omega) = \frac{1}{RCj\omega+1}$